

1 The effect of HDPE and LDPE pyrolytic oils on cavitation 2 formation in a common-rail diesel injector

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14 *Abstract*

15 *Plastic production and usage increase every year due to its practicality, adaptability, and low-cost*
16 *production. The problem with plastic arises when it becomes waste and needs to be treated. Most of*
17 *the plastic we use is produced from petrochemical material that can be used in resource recovery*
18 *processes like pyrolysis to produce various materials. One of the pyrolysis process products is pyrolytic*
19 *oil, whose properties are similar to conventional fuels. Minor differences in fuel properties can*
20 *influence the injection process, in-nozzle flow condition, spray formation and break-up, the*
21 *combustion process, etc. The presented paper aims to study the influence of pyrolytic oil`s properties*
22 *on cavitation formation in the injection nozzle of a common-rail injector. First, the pyrolytic oils were*

23 *obtained from waste high- and low-density polyethylene using a pyrolysis reactor. Afterwards, the oils*
24 *were characterized and implemented in the AVL FIRE computation program for studying their*
25 *influence on cavitation formation in the injection nozzle hole. The obtained results indicate slight*
26 *differences in fuel properties that influence cavitation formation and spread in the injection hole,*
27 *which further influence conditions at the exit of the injection hole. The lower lower viscosity of*
28 *pyrolytic oils influences lower friction in the fuel nozzle flow. The lower density and viscosity of*
29 *pyrolytic oils promotes cavitation formation, advance time of its appearance at injection hole exit and*
30 *influence the shorter presence of cavitation in the needle closing phase.*

31 Key words: plastic waste, pyrolytic oils, cavitation, common-rail, multiphase flow, transient
32 simulation

33 **Introduction**

34 Plastic and plastic products play a significant role in our everyday life. Several traditional materials
35 like steel, wood, etc., have been replaced by plastic materials. This has influenced the rapid increase
36 of plastic production in the recent decade, which reached 368 million tonnes globally in 2019, from
37 which Europe encountered the production of 57.9 million tons of produced plastic. [1] Low
38 production costs, rapid economic growth, and the increase in global populations, are only a few
39 reasons for the constant global growth in plastic production. [2]. Globally, the plastic production
40 compound annual growth rate is 8.4 %. [3] [4]. More than half of global plastic is produced in Asian
41 countries, while Europe was responsible for 16 % of the total global plastic production in 2019. The
42 problem with plastic arises when it becomes waste that needs to be treated. There are several
43 techniques that can be employed for plastic waste treatment. The most conventional process for
44 plastic waste treatment is landfilling, which is still used commonly nowadays. According to [5], about
45 40 % of plastic waste ends in landfill globally. The problem with landfilling of plastic waste is the non-
46 biodegradability nature of plastic materials, which will degrade very slowly in landfill conditions.
47 Additionally, small particles of degraded plastic can come in contact with groundwaters which can

48 lead to contamination of water sources, air, or soil. [6] In Europe, 24.9 % of collected plastic waste
49 was sent to landfilling in 2018, 42.6 % of collected waste plastic was used in energy recovery
50 processes, and 32.5 % was sent to recycling. [1] Waste plastic recycling can be divided further into
51 physical recycling and resource recovery, attracting increasing attention, since it can help us to
52 obtain expensive petrochemical materials that can also be used as fuels. The process of resource
53 recovery is realized mainly using thermolysis processes, from which pyrolysis is used most widely. [7]
54 Pyrolysis is a process in which long-chain polymers are degraded into smaller, less complex molecules
55 at elevated temperatures and in the absence of oxygen. The catalyst can be used further to influence
56 the obtained oil properties. [8] [9] [10] The main products of plastic waste pyrolysis are oil, gas, and
57 solid residue. [11] [12] Since most plastic is still produced from petrochemical materials, [7] the oil
58 produced from plastic waste has properties similar to diesel and gasoline fuels, and can be used in
59 internal combustion engines.

60 Kizza et al. used waste low-density polyethylene (LDPE), high-density polyethylene (HDPE),
61 polypropylene (PP), and polystyrene (PS) to produce plastic derived fuels (PDF) using a pyrolysis
62 process. The viscosity, density and flash point of the fuels were lower than diesel, while the lower
63 heating value of PDF was in a similar range to diesel fuel. They concluded that the produced fuels
64 compared relatively well with conventional diesel fuel properties in Uganda, and could potentially
65 substitute it. [13] Tulashie et al. also used waste PP, HDPE and LDPE plastic to produce PDF using a
66 batch fixed bed pyrolysis reactor. After the characterization, they observed that the obtained fuels
67 properties were in the diesel fuel range, and concluded that pyrolysis of plastic waste presents an
68 efficient and clean method for treating plastic waste. [14] The semi-batch pyrolytic reactor with fixed
69 bed was also used in the study of Mangesh et al. [15] The waste plastic they used was the same as in
70 the work of Tulashie et al. [14], while ZSP-5 zeolite was used as the catalyst. The results of catalytic
71 pyrolysis indicate that some plastic derived fuels (oils) have properties that are very similar to
72 conventional diesel fuel, while others differ slightly from diesel properties. Since the properties of
73 PDF produced from PP plastics have the most diesel like characteristics, they used this oil to produce

74 a 5, 10, and 15% mixture of PP derived PDF with conventional diesel, and tested it in a 4-cylinder,
75 turbocharged diesel engine. The obtained results indicate that the use of PDF from PP plastic as a
76 substitute for conventional diesel leads to higher in-cylinder peak pressure, a higher heat release
77 rate, higher brake specific fuel consumption, a higher exhaust gas temperature, a longer ignition
78 delay and higher emissions of carbon monoxide (CO), carbon dioxide (CO₂), nitrogen oxides (NO_x),
79 and hydrocarbons (HC). [15] Singh et al. [16] used LDPE plastic to produce pyrolytic oil in a fixed bed
80 reactor, and used it to make a 20 % mixture of PDF with conventional diesel fuel. The mixture was
81 used further to run a single-cylinder, naturally aspirated diesel engine, and the obtained results were
82 compared to diesel and pure PDF fuel. The obtained results indicate that the use of pyrolytic oil has a
83 minor influence on in-cylinder pressure, but it decreases engine brake thermal efficiency, increases
84 exhaust gas temperature, CO emissions, HC emissions, NO_x emissions, while decreasing CO₂
85 emissions. Das et al. [17] used medical plastic waste to produce PDF in a batch pyrolysis reactor and
86 used this oil further to run a compression ignition engine with different mixtures of PDF with diesel
87 fuel. They concluded that pyrolytic oils influence engine brake thermal efficiency slightly, but
88 increase CO emissions, HC emissions, NO_x emission, and CO₂ emissions. A similar effect on engine
89 condition was also observed in [18], where mixed plastic was used to obtain pyrolytic oil in a reactor
90 with a fixed bed.

91 As can be seen from the presented literature review, plastic waste can be transformed into synthetic
92 fuels successfully via a pyrolysis process. Their usage in internal combustion engines influences
93 engine performance and the emission formation process. This is usually related to the different
94 chemical composition and physical properties of pyrolytic oils compared to conventional fuels. It is
95 well known that diesel engine performance and the emission formation process are also related to
96 the spray development and spray formation process, which can be affected by the fuel flow
97 conditions in diesel injectors. [19] [20] The fuel flow conditions inside the injector nozzle can be
98 influenced by the injection pressure, which is increased significantly in modern common rail injectors
99 in order to obtain more efficient combustion and to increase engine efficiency. [21] Yu et al. [22]

100 concluded that higher viscosity of the fuel leads to lower cavitation formation inside the fuel injector.
101 The fuel with the highest viscosity had the longest spray penetration length and the narrowest spray
102 jet. [22] Torrelli et al. [23] tested the influence of fuel properties on internal nozzle flow in a five-hole
103 injector. They concluded that fuel properties influence the injector performance and cavitation
104 formation inside the injector. Less viscous fluids have lower friction, resulting in higher fuel velocities,
105 and influencing their mass flow rate at the same pressure. Jiang et al. [24] also found that fuels with
106 lower viscosity are more likely to form cavitation in an injector nozzle.

107 Since the difference in fuel properties can influence fuel flow conditions in a diesel injector nozzle
108 significantly, the presented paper focuses on studying the influence of plastic-derived fuels`
109 (pyrolytic oils) properties on the fuel flow conditions and cavitation inception in a Denso common-rail
110 injector. The study was done using the 3D computational program AVL FIRE, in which transient
111 simulations, which consider full needle movement during the fuel injections, were carried out using
112 the RANS approach. First, the pyrolytic oils were obtained from HDPE and LDPE plastics using a batch
113 reactor with a fixed bed in a nitrogen atmosphere. The obtained oils were characterized further and
114 their properties were compared to conventional diesel fuel and implemented in a computational
115 program. The numerical model was validated compared to the experimental results, and the proper
116 computational mesh was selected in the next Section. Then, numerical simulations were performed
117 using different mixtures of diesel fuel and pyrolytic oils at a constant injection pressure of 845 bar
118 and a constant in-cylinder pressure of 60 bar. The same needle lift profile was used for all fuels. The
119 obtained results indicate that the differences in fuel properties influence cavitation formation inside
120 the injection hole and the condition at the injection hole exit.

121 To the authors' knowledge, the influence of pyrolytic oils on cavitation inception inside the injection
122 nozzle has not been studied extensively. Therefore, we believe that the study can help to understand
123 the behavior of pyrolytic oils on the condition inside the injection nozzle, and can bring their usage in
124 compression ignition engines closer to their implementation.

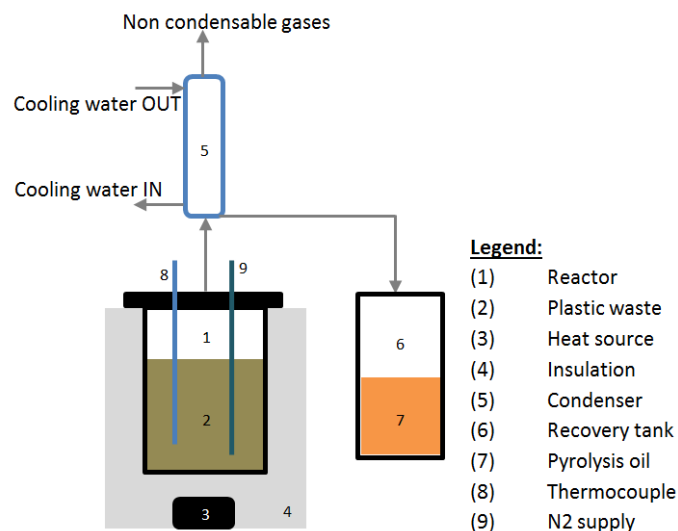
125 **Materials and methods**

126 Plastic Material

127 The plastic used in the presented study was collected from municipal waste at the Faculty of
128 Mechanical Engineering at the University of Maribor. The plastic waste was sorted, and only LDPE
129 and HDPE plastics were used for obtaining oily pyrolytic. The collected plastic was washed and dried
130 before it was cut into smaller pieces.

131 Pyrolysis Oil Production

132 A single batch pyrolytic reactor with a fixed bed was used for liquid oils` production in the presented
133 study. The set of the pyrolysis process experiment is presented schematically in Figure 1. The used
134 plastic waste was inserted into the reactor chamber, which was sealed and insulated with a glass
135 wool jacket. The temperature inside the reactor was monitored using a K-type thermocouple and a
136 National Instruments DAQ carrier WLS-9163 and NI-9219 module. Before each experiment, nitrogen
137 gas (N2) was used to flush the whole system and to eliminate any potential air pockets out of system.



139 **Figure 1: Pyrolysis process experiment set-up**

140 The pyrolytic process was carried out at a 400°C reactor temperature. The produced vapors flow into
141 the condenser, where the majority of it condenses. The obtained pyrolytic oils were collected in a

142 recovery tank and were removed at the end of the process. Non condensable gases were released
 143 into the atmosphere, and the solid residue was removed from the reactor chamber after each
 144 experiment.

145 Oils characterization

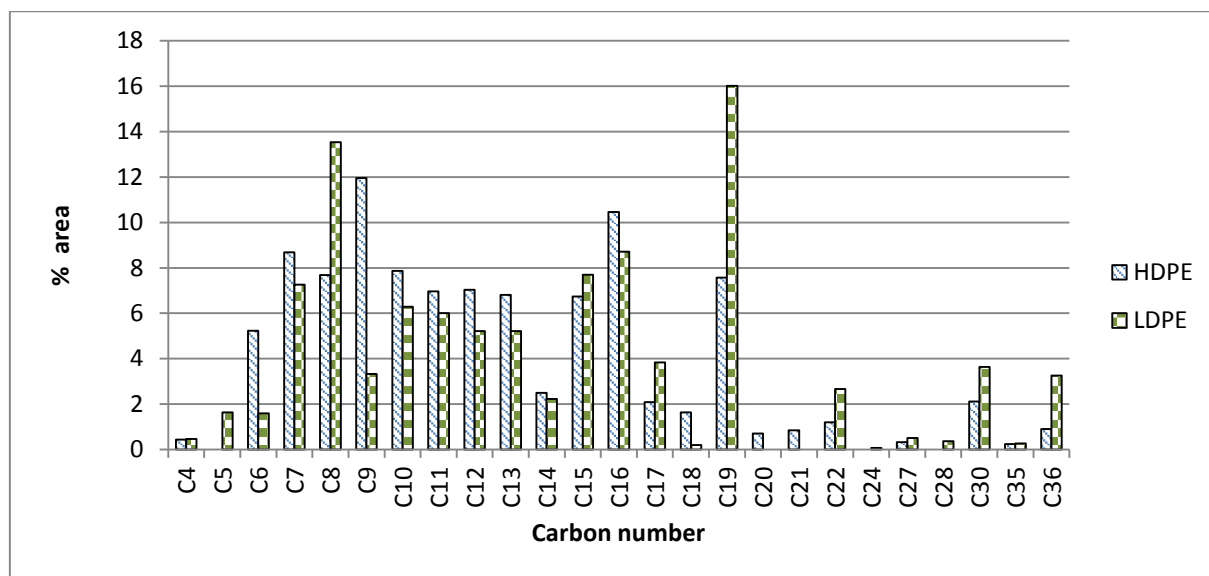
146 The properties of fuels play a significant role in their use. If fuels want to be used as road propulsion
 147 fuel for compression ignition engines in the European Union, they must meet the EN 590 Standard
 148 for diesel fuel. The following section of the manuscript presents some properties of the obtained PDF
 149 and their comparison to conventional diesel fuel.

150 The presented study does not focus on optimizing the pyrolysis process or decrease of energy
 151 consumption during the process, so the ratios of pyrolysis products and energy balance were not
 152 included in the presented work. The properties of the obtained pyrolytic oils from HDPE and LDPE
 153 plastics and the properties of diesel fuels required by the EN 590 Standard are presented in Table 1.

154 **Table 1: Fuel properties [8]**

	D2 EN 590	HDPE	LDPE
Density at 15°C [kg/m ³]	820-845	770.40	775.40
Surface tension [mN/m]	26.80	23.20	23.00
Calorific value [MJ/kg]	42.8-43.4	46.43	46.54
Kin. Viscosity [mm ² /s]	2.0-4.5	1.32	1.53
Cetan index	51.8	63.97	64.38
CHNO content [%w/w]	86.13 C	78.44 C	80.91 C
	13.87 H	13.40 H	13.53 H
	0 N	0.21 N	0.20 N
	0 O ₂	7.94 O ₂	5.35 O ₂

156 Figure 2 presents the results of the carbon number distribution for the obtained pyrolytic oils. As can
157 be seen from the results, the obtained oils consist of hydrocarbons with carbon numbers in the range
158 C4 to C36, with the majority in the range of C6 to C19. This is in good agreement with diesel fuel,
159 which has a carbon number distribution in the range from C8 to C23. [27][28]

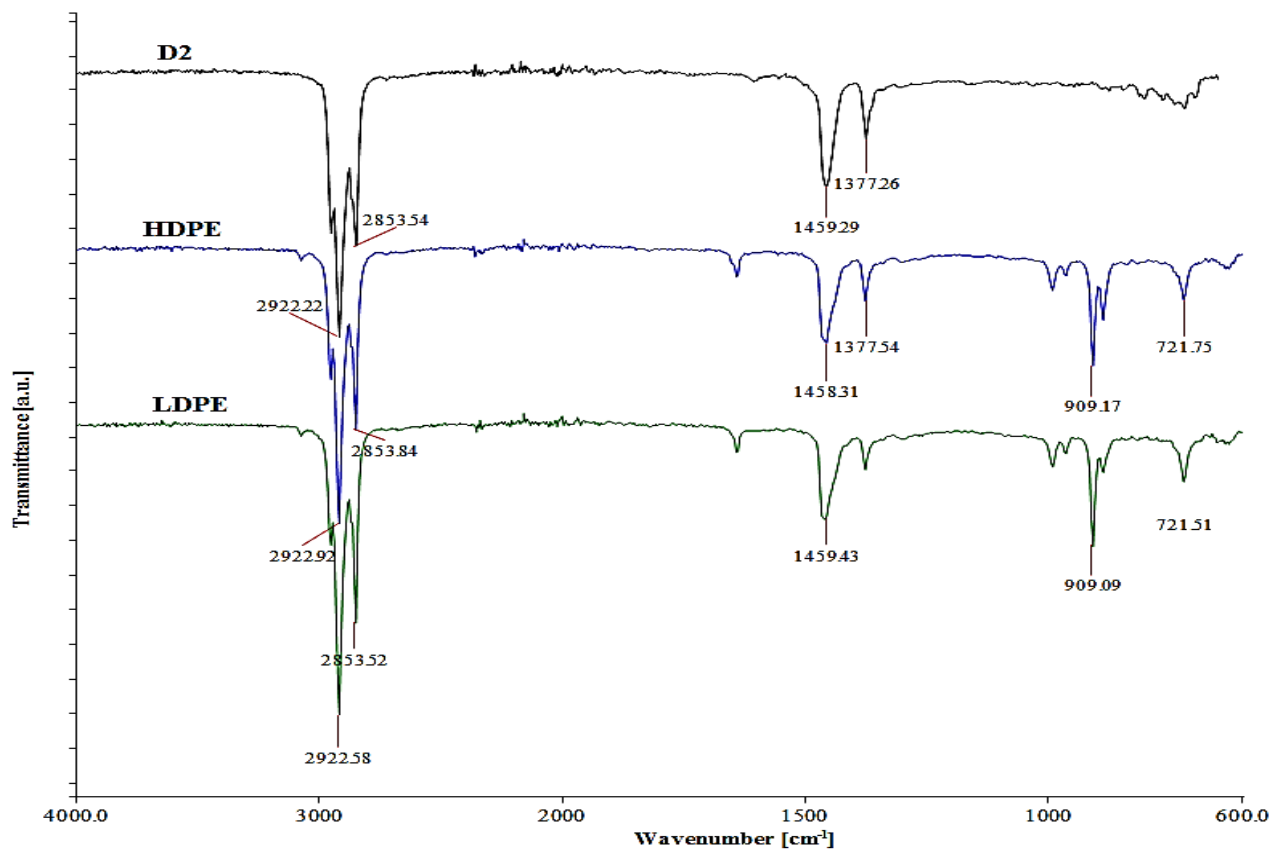


160

161 **Figure 2: Carbon number distribution**

162

163 The results of ATR the FT-IR spectra recorded for the obtained oils are presented in Figure 3.



164

165 **Figure 3: ATR FT-IR spectra of conventional diesel fuel (D2) and the pyrolysis oils of HDPE and LDPE**

166 The ATR FTIR spectra of conventional diesel fuel (D2) and pyrolysis oils from HDPE and LDPE showed
 167 the typical signals of aliphatic hydrocarbons in the range from 2960 cm^{-1} to 2850 cm^{-1} , at 1460 cm^{-1}
 168 and at 1375 cm^{-1} , respectively, which are due to the presence of $-\text{CH}_3$ and $-\text{CH}_2$ groups. In addition to
 169 the above signals, the typical signals for olefins were detected in the spectra of the pyrolysis oils of
 170 HDPE and LDPE, at 3079 cm^{-1} , 1643 cm^{-1} , 991 cm^{-1} and 909 cm^{-1} . The mentioned signals were less
 171 intense.

172 Fuels` properties for simulations

173 The properties of the fuel mixtures where calculated from the obtained properties of the HDPE and
 174 LDPE pyrolytic oils presented in Table 1: Fuel properties [8]. Table 2 presents the properties of the
 175 fuels that were used in the numerical simulations. According to [25] [26], a sharp drop of pressure at
 176 the nozzle hole entry is so rapid that the absolute value of the fuel saturation pressure is of minor

177 influence on cavitation occurrence. Due to this finding, the saturation pressure for all fuels was the
178 same.

179 **Table 2: Fuel properties used in the simulations**

	D2	HDPE	LDPE	HDPE_50	LDPE_50	HDPE_25	LDPE_25	HDPE_10	LDPE_10
Density at 15°C [kg/m ³]	830	770.40	775.40	800.20	802.70	815.10	816.35	824.04	824.54
Surface tension [mN/m]	26.8	23.20	23.00	25.00	24.90	25.90	25.85	26.44	26.42
Kin. Viscosity [mm ² /s]	2.14	1.32	1.53	1.73	1.83	1.94	1.99	2.06	2.08

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181

182

183 **Experimental set-up**

184 Injection system

185 A Denso diesel injector, model 7H150 with solenoid valve and seven injection holes, was used in the
186 presented work. All injection holes had the same length of 0.76 mm and diameter of 0.15 mm. A
187 detailed description of the experimental set-up was presented in [19].

188 Engine

189 The injector was taken from 4-cylinder Nissan YD22 engine. The main properties of engine are
190 presented in

191 **Table 3: Properties of test engine**

Properties	Value
Engine displacement [l]	2.184

Max. power [kW]	82 (@4000 min ⁻¹)
Max. torque [Nm]	248 (@2000 min ⁻¹)
Compression ratio	16.7/1
Bore [mm]	86.5
Stroke [mm]	94

192

193 Operating regime

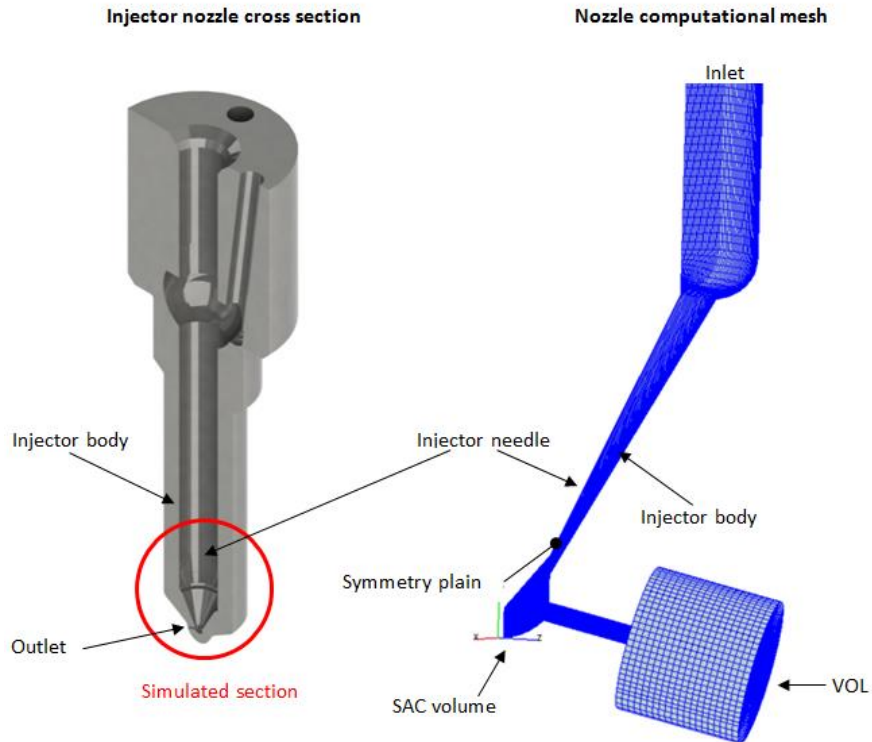
194 The operating regimes were obtained during the experimental measurements. The selected engine
195 operating regime for this work was 1700 rpm, 110 NM of torque, BMEP 6.33 bar, 845 bar of injection
196 pressure and 60 bar of in-cylinder back pressure. The total injection time was 1.26 ms. [19,29,30]

197 **Numerical model**

198 Model

199 The numerical model was made for one injection hole (one seventh of the whole injector). Additional
200 volume (marked with VOL on Figure 4) was placed at the outlet of the injection nozzle. The volume is
201 used for boundary condition definition, and allows us to avoid defining the boundary condition at the
202 nozzle hole exit. According to the program provider we get more realistic physical initialization and
203 results at the nozzle outlet when using this method for outlet boundary condition definition.

204



205

206

Figure 4: Injector nozzle model cross-section and computational mesh

207

208 Mesh independence study

209 The mesh independence study was carried out in order to estimate the numerical error. The
 210 Richardson extrapolation method was used to determine the grid convergence index (GCI), which
 211 provides a uniform measure of convergence for the grid refinement studies, and presents an
 212 estimate of the discretization error. [31,32] The average fuel velocity and turbulent kinetic energy
 213 (TKE) at the outlet were monitored on three different meshes with different numbers of elements.
 214 The study was done with the injection needle half open. The results of the mesh independence study
 215 are presented in Table 3.

216 **Table 4: Mesh independence study**

Mesh	Number of	Average velocity at the	Average turbulence kinetic energy at
------	-----------	-------------------------	--------------------------------------

	elements	outlet [m/s]	the outlet [J/kg]
Coarse (1)	138175	282.87	518.27
Medium (2)	358996	287.38	801.83
Fine (3)	1582816	257.46	856.25
GCI _{fine} [%]	-	4.26	0.541
GCI _{medium} [%]	-	1.23	9.06

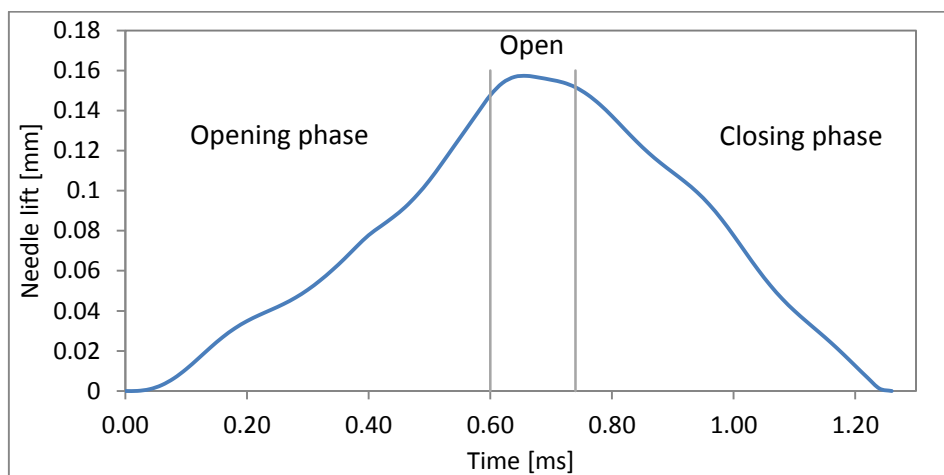
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218 Following the results of the mesh independence study, the medium mesh with 358,996 elements was
 219 used for further work. The additional refinement of the mesh provides slightly better results, but
 220 increases the calculation time significantly.

221 Simulation set-up

222 The time (physical) of simulation was equal to the total injection time obtained during the
 223 experimental work. The time was 1.26 ms, and was the same for all the simulation. The timesteps in
 224 the simulation were smaller at the start of simulation (2.5×10^{-8} s) and larger (5.0×10^{-8} s) at the end
 225 of simulation. This configuration provided good convergence during the whole simulation. The
 226 injection pressure of 845 bar was defined at the inlet. The in-cylinder back pressure of 60 bar was
 227 defined in the volume (VOL) added to the numerical model of the injector. The symmetry boundary
 228 condition was used on the sides of the injector body. The properties of the tested fuels are presented
 229 in Table 1, and were implemented in the computational program.

230 The transient needle movement was defined during the simulation. The needle lift during the
231 injection was the same for all fuels, and was defined in [19]. The needle lift process is split into three
232 phases, and is presented in Figure 5. The first is the needle opening phase, which begins with the
233 start of needle lift and ends at 0.6 ms when the needle is more than 95 % open. It is followed by the
234 open phase, when needle is fully open (more than 95% of full needle lift). At 0.74 ms the closing
235 phase of the needle lift starts, and ends with the needle being fully closed at 1.26 ms.



236

237

Figure 5: Needle lift

238 At the start of the simulation, the needle in the numerical model was not fully closed. This allowed
239 avoiding the zero thickness cells, and enabled us to determine the computational mesh in the whole
240 model. The minimal distance between the injector body and the needle was 1 μm .

241 Mathematical models

242 The simulations of unsteady, multi-phase flow inside the injector were performed using the Eulerian-
243 Eulerian approach. The two-fluid model approach was used, which calculates all the conservation
244 equations for each phase and is integrated in the AVL FIRE computational program. Mass (eq. (1)),
245 momentum (eq. (2)) and energy (eq. (3)) conservation equations were considered during the
246 calculation. Additional to the conservation equations, a Linear cavitation model was used to calculate
247 the mass and momentum exchange on the phases' interface. The changes of fuel density with

248 pressure were calculated using the Tait equation (4), while turbulence modeling was done using a
 249 standard k-ε turbulent model with hybrid wall treatment, which is suitable for all y+ values. [33] The
 250 equations are presented in Table 4.

251 **Table 5: Used mathematical models [33]**

$\frac{\partial \alpha_k \rho_k}{\partial t} + \nabla \cdot \alpha_k \rho_k v_k = \sum_{l=1, l \neq k}^2 \Gamma_{kl}$	Mass
eq. (1)	
$\begin{aligned} \frac{\partial \alpha_k \rho_k v_k}{\partial t} + \nabla \cdot \alpha_k \rho_k v_k v_k \\ = -\alpha_k \nabla p + \nabla \cdot \alpha_k (\tau_k + \tau_k^t) + \alpha_k \rho_k g + v_k \sum_{l=1, l \neq k}^2 \Gamma_{kl} \\ + \sum_{l=1, l \neq k}^2 M_{kl} \end{aligned}$	Momentum
eq. (2)	
$\begin{aligned} \frac{\partial \alpha_k \rho_k h_k}{\partial t} + \nabla \cdot \alpha_k \rho_k v_k h_k \\ = \nabla \cdot \alpha_k (q_k + q_k^t) + \alpha_k \rho_k q_k''' + \alpha_k \rho_k f \cdot v_k \\ + \nabla \cdot \alpha_k (\tau_k + \tau_k^t) \cdot v_k + \alpha_k \frac{\partial p}{\partial t} + \sum_{l=1, l \neq k}^2 H_{kl} + \sum_{l=1, l \neq k}^2 h_{kl} \Gamma_{kl} \end{aligned}$	Energy
eq. (3)	
$\rho_l = \rho_{ref} \sqrt[n]{\frac{p + B}{p_{ref} + B}}$	Tait
eq. (4)	

$$\Gamma_{12} = \rho_d N''' 4\pi R^2 \dot{R} = \Gamma_{21}$$

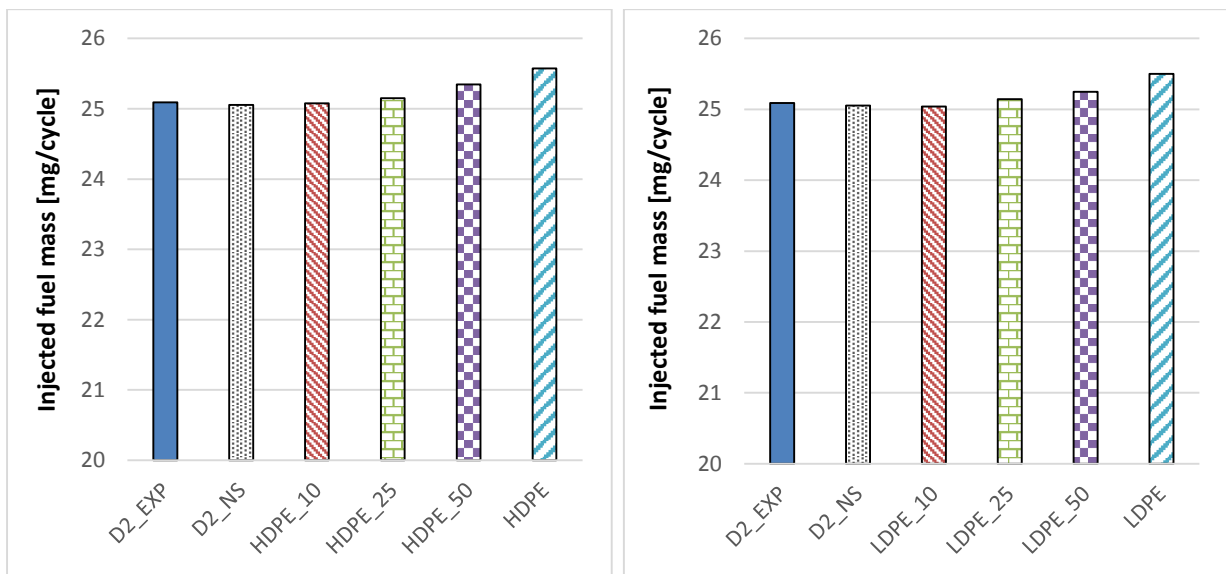
Interfacial mass
exchange
eq. (5)

252

253 Results

254 The following Section presents the results of fuel properties` influence on the injection properties
255 and in nozzle flow conditions in the used common rail diesel injector.

256 Figure 6 present the results of the total injected fuel mass for all tested fuels and for the
257 experimentally obtained results. Numerical (simulated) obtained results are marked with
258 abbreviation NS while experimental results are marked with abbreviation EXP.



259 **Figure 6: Comparison of injected fuel mass**

260 From the results presented in Figure 6 we can see that the numerical simulation predicts the total
261 injected fuel mass in one injection cycle precisely. The difference between the numerical and
262 experimentally obtained results of total injected fuel mass for diesel fuel is less than 1 %. The

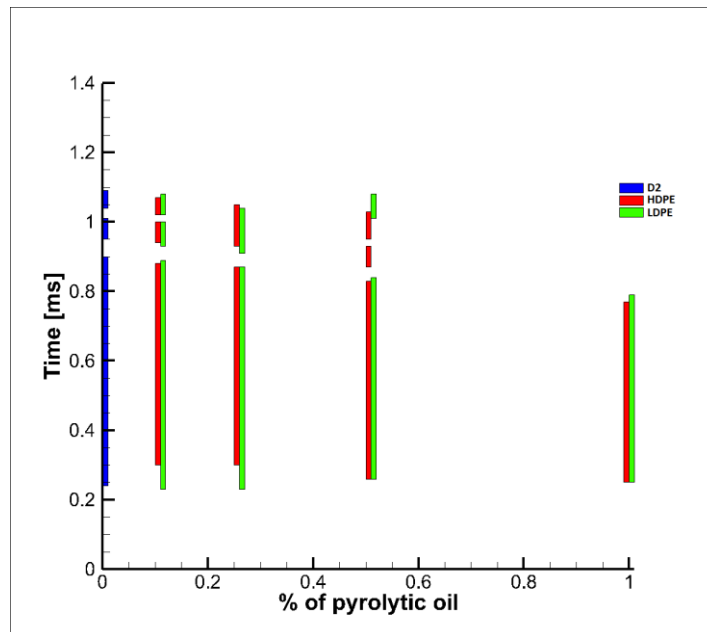
263 presented results also indicate that adding plastic derived fuel to diesel fuel has an influence on the
264 increased total injected fuel mass.

265 In-Nozzle Flow and Cavitation Inception

266 In the following chapter only the most relevant numerical results are presented at different times
267 during the injection process.

268 When fuel flows through the injection nozzle it undergoes significant changes which influence local
269 flow velocity and pressure. There are two distinctive areas where cavitation is usually formed. The
270 first is under the injection needle, where the cavitation is formed during an early stage of needle
271 opening and at the last steps of needle closing, due to the very narrow gap between the injector
272 needle and the needle seat. This gap increases fuel flow velocity and decreases its pressure, which
273 induces the formation of cavitation. The second area is at the injection hole entry, where the fuel
274 undergoes significant changes in flow direction: This from an area, usually in the upper part of the
275 injection nozzle hole, where the pressure drop is very high (almost to the value of 0 Pa of absolute
276 pressure [34]), and induces cavitation formation. In the presented study, we have focused only on
277 studying the cavitation formation in the injector's injection hole.

278 Figure 7 present the time when cavitation structures are present in the computation domain of the
279 injector's nozzle hole during the injection process.



280

281

Figure 7: Appearance of cavitation in the injection hole

282 As can be seen from Figure 7, cavitation in the injection hole starts to form between 0.25 and 0.30
 283 ms after the injection starts. Then it starts to dissipate (collapse) around 0.77 ms after the start of
 284 injection, and depending on the used fluid, reappears again after around 1 ms of the injection
 285 process. From the presented results we can see clearly that the cavitation inside the injection nozzle
 286 fluctuates during the closing phase of the injection process.

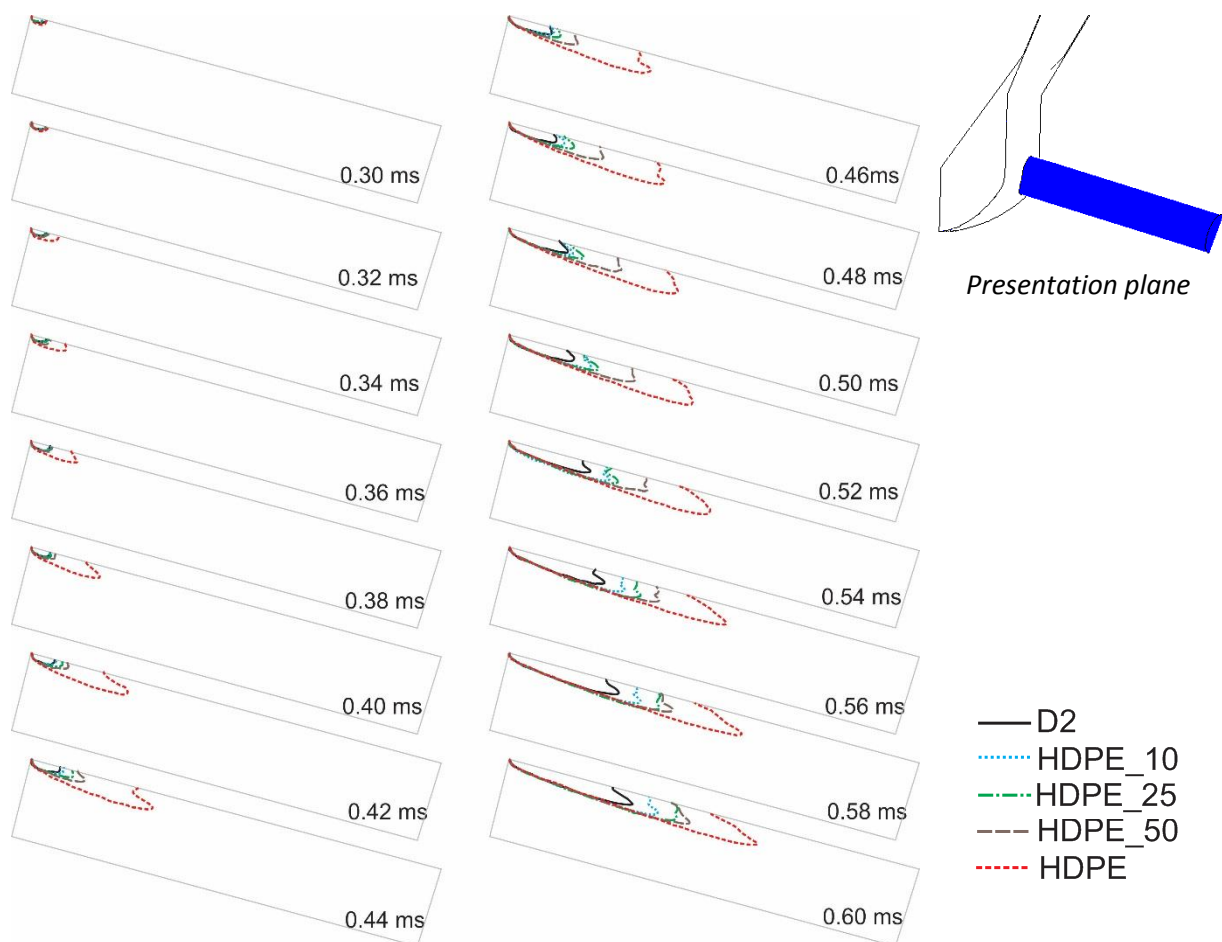
287 **Needle opening phase**

288 From the results presented in Figure 7 we can see that cavitation starts to form in the needle
 289 opening phase, and is present constantly for all fuels up to the needle closing phase.

290 Figure 8 and Figure 9 present the results of cavitation development on a plane positioned in the
 291 middle of the injection hole for the needle opening phase. The presentation plane is presented
 292 schematically in the upper right corner of all Figures presenting cavitation development on the
 293 middle plane of the nozzle injection hole. The results are presented for time intervals from 0.3 ms up
 294 to 0.64 ms of the needle opening phase, with time increments of 0.02 ms. Before 0.3 ms there was
 295 hardly any difference in the contours of the cavitation, so the results are not included. Only the

296 contours of cavitation structures are shown, for better presentation. This presentation gives us an
297 insight into cavitation formation and spread through the injection hole during the needle opening
298 phase.

299

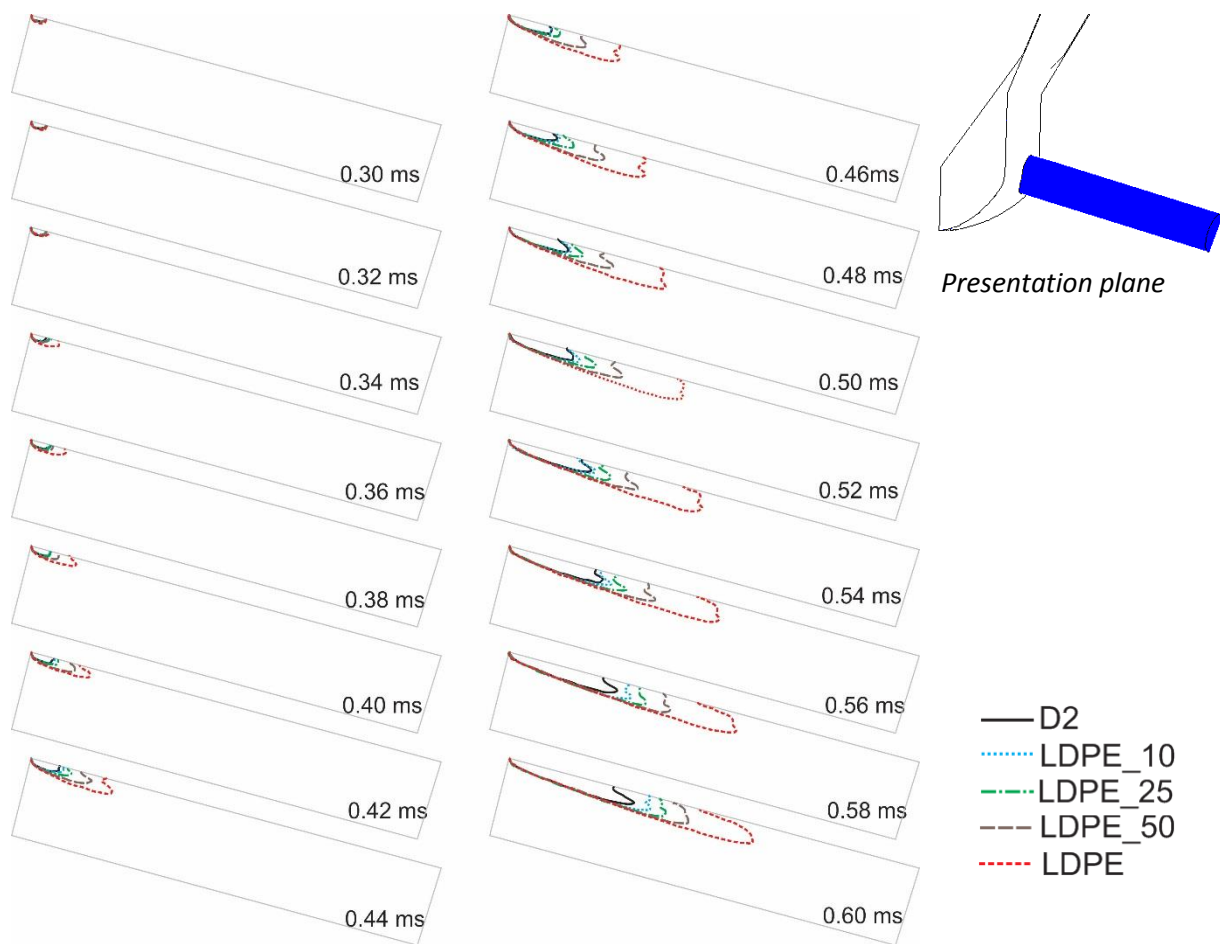


300

301 **Figure 8: Contours of cavitation development for diesel fuel, HDPE fuel and their mixtures during the needle opening**
302 **phase**

303 The transition from non-cavitation to cavitating flow in the needle opening phase for diesel fuel,
304 HDPE pyrolytic oil and their mixtures are presented in Figure 8. At 0.30 and 0.32 ms the contours for
305 all fuels have the same shape and length. At 0.34 ms of injection time we obtained rapid formation
306 and spread of cavitation contours for the HDPE oil, followed by significantly slower growth of

307 HDPE_50, HDPE_25, HDPE_10 and diesel fuel cavitation structures. The ratios between the tested
 308 fuels stayed more or less the same till the end of the needle opening phase. Since the boundary
 309 conditions in all simulations were the same, the difference in cavitation development was influenced
 310 by the differences in fuel properties. Pyrolytic oil and their mixtures have lower viscosity compared
 311 to diesel fuel, which can influence higher fuel velocity due to lower friction [23], while higher
 312 viscosity of diesel fuel also influences slower formation of cavitation structures in the needle
 313 opening phase. This influences faster formation and spread of plastic derived fuels` cavitation
 314 structures through the injection hole.



315 **Figure 9: Contours of cavitation development for diesel fuel, LDPE fuel and their mixtures during the needle opening**
 316 **phase**

317 The results for the cavitation development of LDPE pyrolytic oil and their mixture with diesel fuel,
 318 presented in Figure 9, show similar trends as the results for HDPE oil. The difference between the

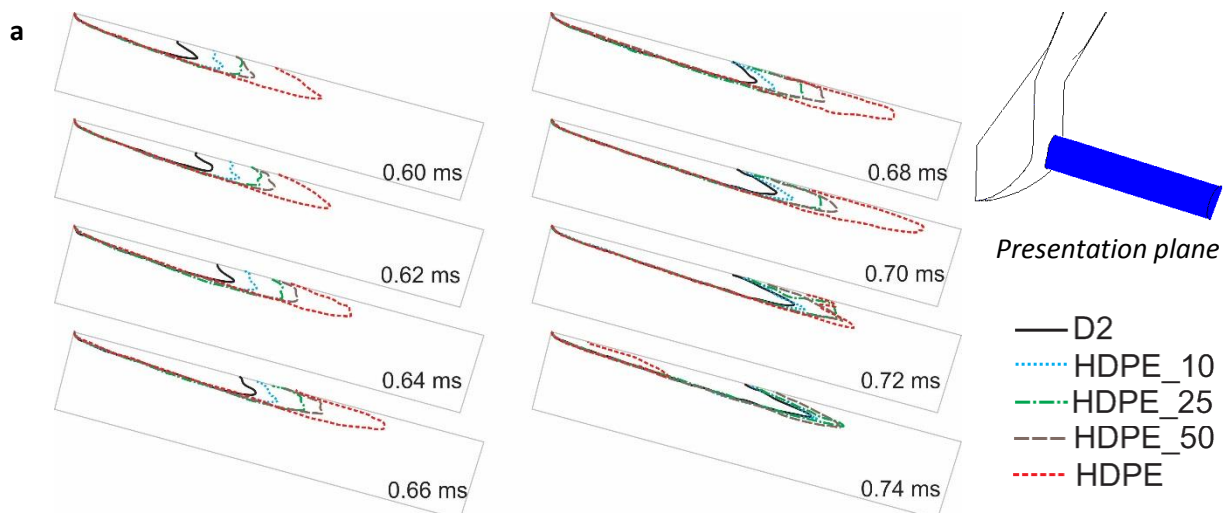
319 cavitation structures` formation and spread through the injection hole started to occur at 0.36 ms of
320 injection. The lower density and viscosity of LDPE pyrolytic oil influenced the faster formation and
321 faster spread of cavitation structures through the injection hole. The longer cavitation structures of
322 PO and its mixtures stayed present till the end of the needle opening phase.

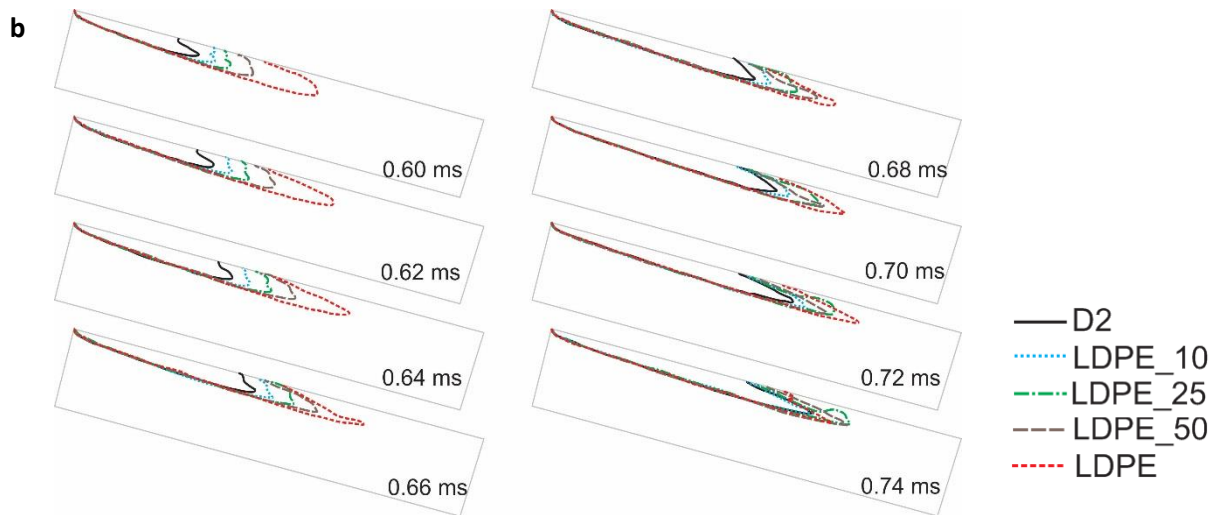
323 Comparing the differences between pure pyrolytic oils, we can notice that the lower density and
324 viscosity of HDPE pyrolytic oil influence the faster formation and spread of cavitation structures in
325 the early stage of needle opening, up to 0.50 ms. From 0.52 ms on there was no visible difference in
326 the length of the cavitation structures` contours for pure HDPE and LDPE pyrolytic oils.

327 **Phase of open needle**

328 The phase of open needle presents the time during the injection process when the needle is fully
329 open (more than 95% of maximal needle lift). Figure 10 presents the contours of the cavitation
330 structures in the nozzle hole for the HDPE and LDPE pyrolytic oils and their mixtures during the
331 needle open phase.

332





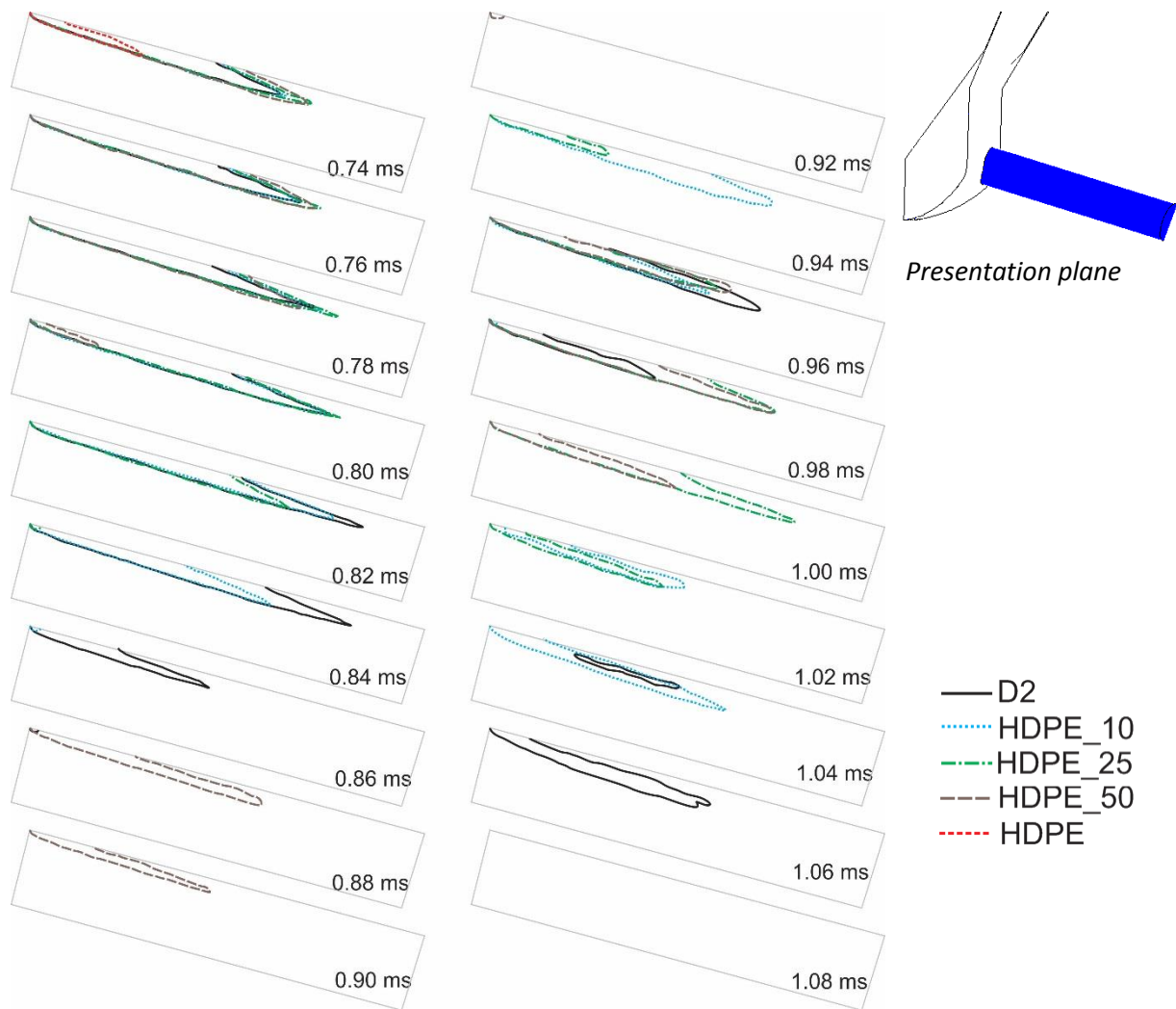
333 **Figure 10: Contours of cavitation development for diesel fuel, HDPE fuel (a), LDPE fuel (b) and their mixtures during the**
 334 **phase of open needle**

335 The results presented in Figure 10 indicate that cavitation structures continue to form and spread
 336 through the injection hole in the phase of open needle. This phenomenon is more rapid for fuels with
 337 lower density and viscosity, which influence the time when each fuel obtains the maximal length of
 338 cavitation structure. In Figure 10 a we can see that, for pure HDPE oil, this occurred at 0.70 ms after
 339 the injection start, and for pure LDPE oil at 0.74 ms, Figure 10 b. The cavitation structures for all
 340 other fuel mixtures and for pure D2 continued to grow and spread at the end of the needle open
 341 phase.

342 **Needle closing phase**

343 The last part of the injection process is the needle closing phase. The results of cavitation structures'
 344 contours in this phase are presented in Figure 11 and Figure 12. Only results up to 1.08 ms are
 345 presented, since there is no visible cavitation after that. After that there is no visible cavitation on the
 346 presentation plane.

347

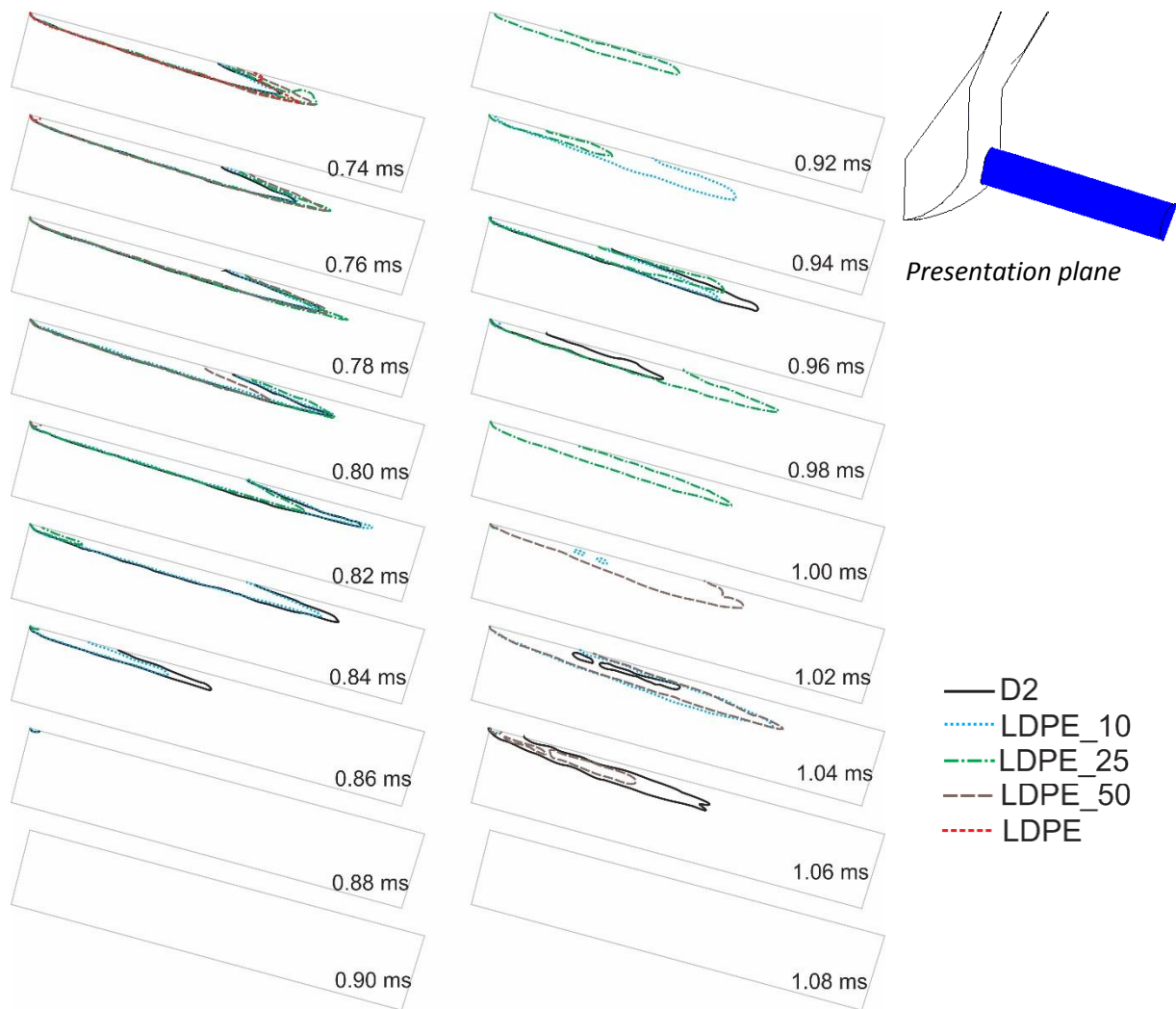


348 **Figure 11: Contours of cavitation development for diesel fuel, HDPE fuel and their mixtures during the needle closing**
 349 **phase**

350 During the needle closing phase the cavitation structures for diesel fuel and for fuel mixtures
 351 continued to form, and spread through the injection hole till they reached maximal length. For the
 352 HDPE_50 mixture this occurred at 0.76 ms, for the HDPE_25 mixture at 0.78 ms, at 0.80 ms for the
 353 HDPE_10 mixture, and at 0.82 ms for the pure diesel fuel. The growth and formation of cavitation
 354 structures is again associated with the differences in fuels properties, and is more rapid for fuel
 355 mixtures which have lower density and viscosity compared to pure diesel fuel, which is in line with
 356 the results presented in [35]. The maximal length of cavitation structures is also influenced by fuel
 357 properties. The presented results indicate that higher fuel density and viscosity increase cavitation
 358 structure length, which was the longest for pure diesel fuel. Figure 11.

359 Once cavitation structures reach their maximal lengths they start to dissipate rapidly and dissipate
360 completely in about 0.04 ms after they achieve maximal values. For pure diesel fuel, cavitation
361 structure collapse occurs in 0.06 ms after maximal length. At 0.88 ms after the injection start the
362 fluctuations of cavitation structures are visible in the injection hole at different times of the injection
363 process for all fuel mixtures and for pure diesel fuel, but not for pure HDPE pyrolytic oil. Figure 11.

364 The same trends were also obtained for LDPE pyrolytic oil and its mixtures with diesel fuel. Figure 12.
365 The cavitation structures for the pure LDPE_50 fuel mixture reached its maximal length at 0.76 ms, at
366 0.78 ms for LDPE_25, and at 0.82 ms for both LDPE_10 and pure diesel fuel. The longest cavitation
367 structures were obtained for pure diesel fuel and its 10 % mixture with LDPE (LDPE_10), which again
368 indicated that higher fuel density and viscosity increase the maximal length of the cavitation
369 structures. The dissipation of cavitation structures again occurred in 0.04 ms after its maximal length
370 was achieved for pure LDPE pyrolytic oil, and in 0.06 ms for pure diesel fuel and its mixtures with
371 LDPE oil.



372 **Figure 12: Contours of cavitation development for diesel fuel, LDPE fuel and their mixtures during the needle closing**
 373 **phase**

374 At 0.92 ms the fluctuation of the cavitation structures were again visible in the injection hole at
 375 different times of the injection process for all fuel mixtures and for pure diesel fuel, but not for pure
 376 LDPE pyrolytic oil. Figure 12. The differences in flow conditions in the injection hole during the needle
 377 closing phase for different fuel were also observed in [25]. The authors of this study concluded that
 378 fuel with lower density and lower viscosity responds faster to needle motion (closing) and behaves
 379 less inertly compared to fuel with higher density and higher viscosity. They associated this
 380 phenomenon to less resistance of fuel to disturbance if its viscosity is lower. Since the HDPE and
 381 LDPE pyrolytic oils have significantly lower fuel viscosity compared to diesel fuel, they are less

382 resistant to disturbances in fuel flow caused by needle closing, which we believe results in no
383 cavitation fluctuation in the final stage of the needle closing phase.

384 Since the cavitation structures are present longer into the needle closing phase when fuel density
385 and viscosity are higher due to their later appearance, the choked flow, caused by the cavitation
386 cloud, is still present in the injection hole when the fuel flow starts to decline due to needle closing.
387 The choked flow can cause a local increase in fuel flow velocity, which can further influence the
388 pressure field inside the nozzle hole. So, the combined effects of fuel density influence on resistance
389 to disturbance to needle closing and later appearance of cavitation structures in the needle closing
390 phase, can influence rebound cavitation. This can be seen as fluctuation of the cavitation structures
391 close to the injection hole walls. This phenomenon is commonly seen in bubble collapse near the
392 wall. [36]

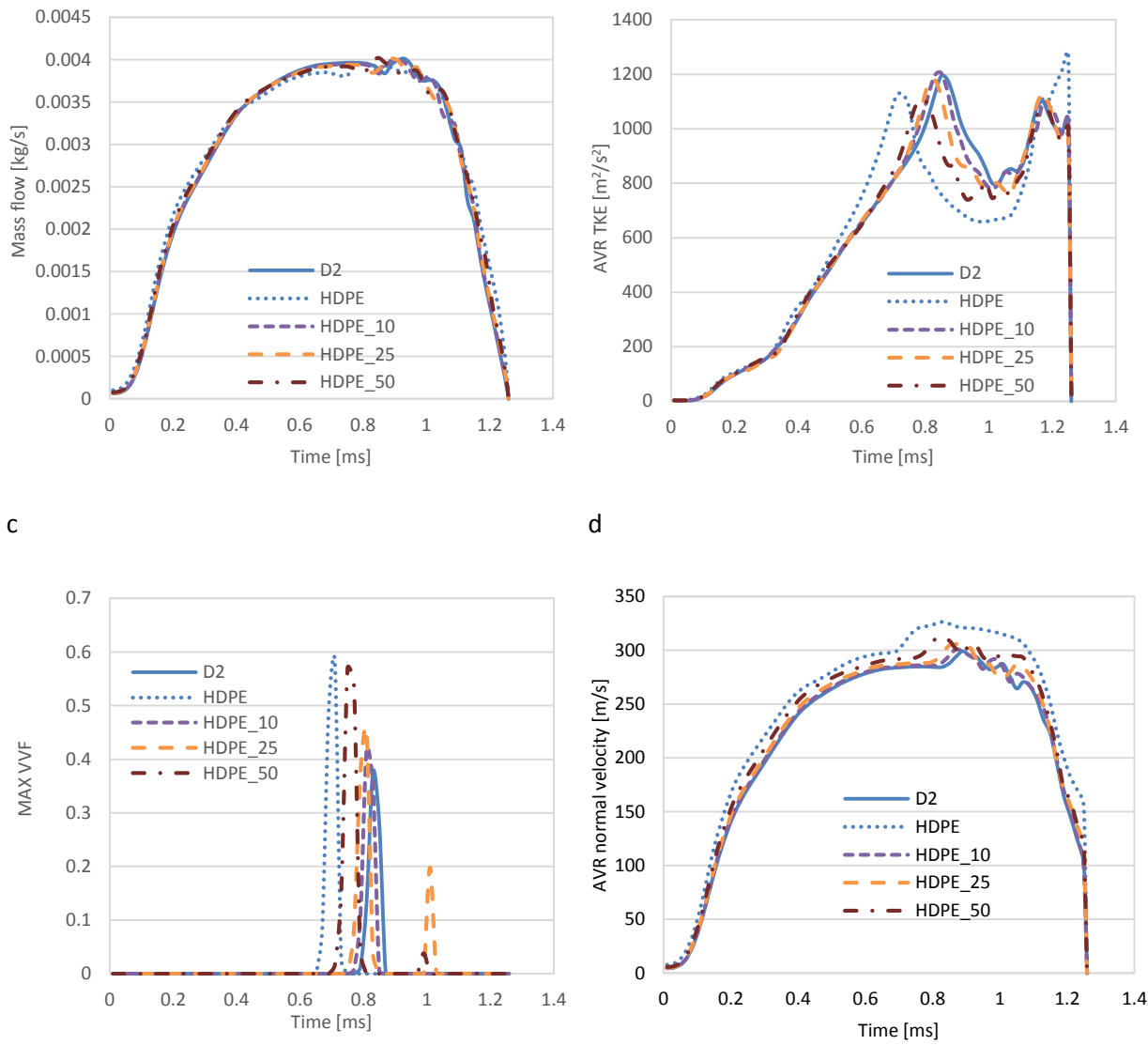
393 Nozzle hole exit

394 The conditions at the nozzle hole exit are very important, since they have a high influence on fuel
395 spray development and break-up. The disturbances of fuel flow at the nozzle hole exit are the results
396 of fuel flow upstream conditions and cavitation inception.

397 Figure 13 and Figure 14 present the integral values of the fuel mass flow rate, the average value of
398 turbulent kinetic energy (AVR TKE), the maximal values of vapor volume fraction - cavitation phase
399 (MAX VVF), and the average values of normal velocity for one injection hole exit.

a

b



400 **Figure 13: Outlet integral quantities for one injection hole (a) Mass flow rate; (b) Average value of fuel turbulent kinetic**
 401 **energy; (c) Maximal value of Vapor Volume Fraction; (d) Average normal velocity for HDPE fuel and their mixtures**

402

403 The results for the fuel mass flow of pure HDPE oil and their mixtures with diesel fuel are presented
 404 in Figure 13. As we can see from the results, there is no significant difference for the mass flows of
 405 pure diesel, pure HDPE oil and their mixtures. In the needle opening phase, the mass flow for all fuels
 406 is increasing without fluctuations, in addition to which, mass flows for all fuels are steady without
 407 fluctuations, except for pure HDPE, where fluctuations in the mass flow rate started to occur at the
 408 end of the needle open phase. In the needle closing phase, the mass flow rate for all fuels started to
 409 decrease due to needle closing. There are visible fluctuations in all fuels` mass flows. The amplitudes

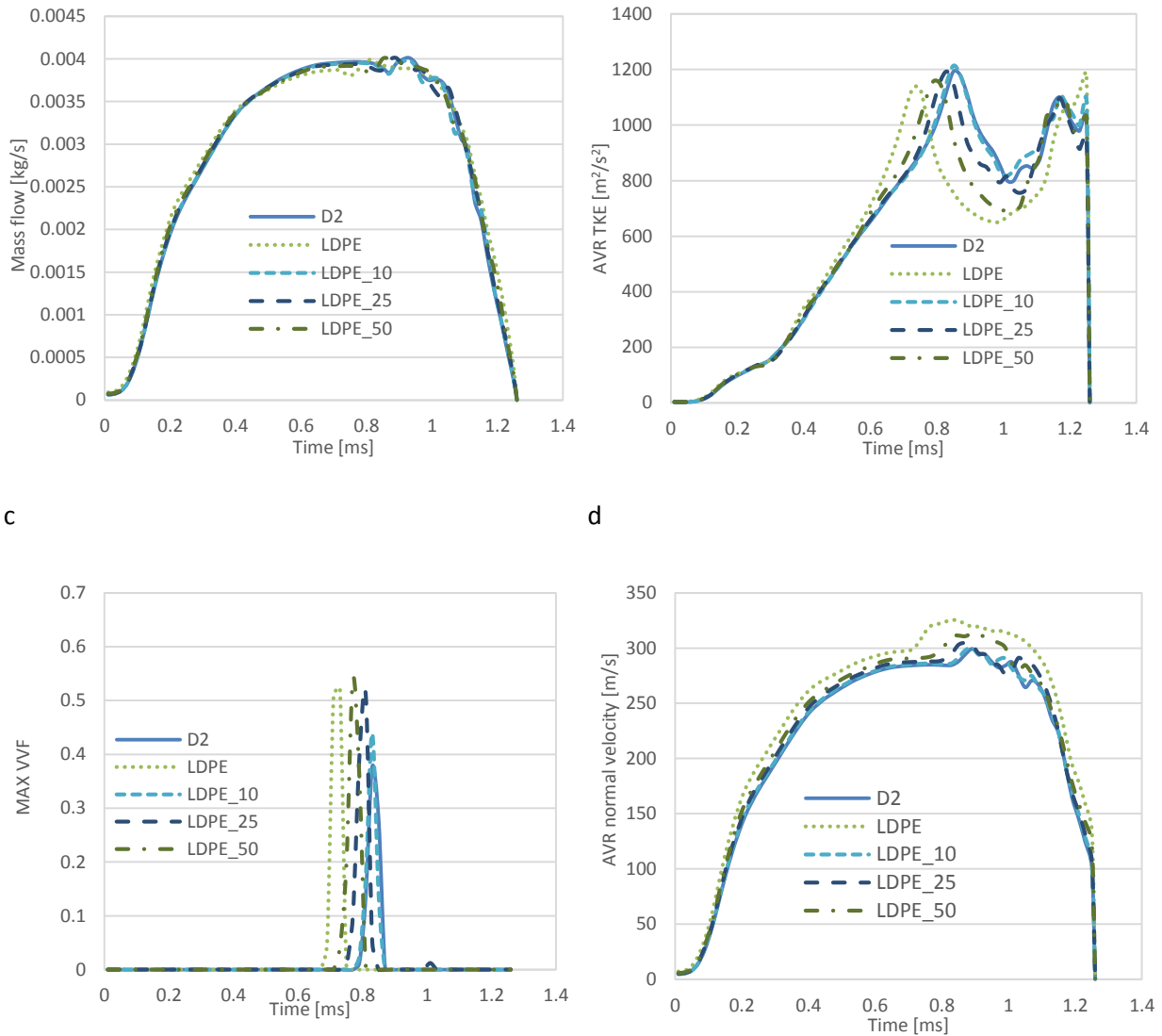
410 of fluctuations are the highest for pure diesel fuel, followed by fuel mixtures and pure HDPE oil. The
411 timing of mass flow fluctuations coincides with the occurrence of cavitation structures at the nozzle
412 hole exit (Figure 13 c). Since the maximal values of VVF for pure diesel fuel and fuel mixture are
413 smaller compared to pure HDPE fuel (Figure 13 c), the authors assume that the amplitudes of
414 fluctuations also depend on the fuel properties.

415 The cavitation phase occurs at the needle hole exit at different times, depending on the fuel. It first
416 appeared for pure HDPE oil, followed by HDPE_50, HDPE 25, HDPE_10 fuel mixtures, and, at the end,
417 by pure diesel fuel. The results coincide with the results of cavitation formation inside the injection
418 hole, where the cavitation started to form first for fuel with lower density and viscosity.

419 The results also show that the average values of fuels TKE increases with the increase of fuels` mass
420 flow rates, and that the peaks of the average TKE at the nozzle hole exit coincides with the time of
421 cavitation structures` occurrence at the nozzle hole exit. This indicates that the formation and spread
422 of cavitation structures influence the increased fuel TKE at the nozzle hole exit. The same trend is
423 evident for the fuel normal velocity at the nozzle hole exit. When cavitation structures occur at the
424 nozzle exit, high fluctuation are obtained in the fuels` normal velocity. The results also show that the
425 velocities for pure HDPE oil and their mixtures are higher than for pure diesel fuel. This is because of
426 the low viscosity of pyrolytic oil and its mixtures, which decrease the friction of the fuel flow. This
427 phenomenon also explains why there are no significant difference in the fuels` mass flow rates.

a

b



428 **Figure 14: Outlet integral quantities for one injection hole (a) Mass flow rate; (b) Average value of fuel turbulent kinetic**
 429 **energy; (c) Maximal value of Vapor Volume Fraction; (d) Average normal velocity for LDPE fuel and their mixtures**

430 The same trends are also seen for LDPE oil and their mixtures with diesel fuel Figure 14. During the
 431 needle opening phase the mass flow of fuels increases without any fluctuations in fuel flow. For pure
 432 LDPE pyrolytic oil the fluctuations in fuel mass flow occurred in the needle open phase, while, for
 433 other fuels, at the start of the needle closing phase. The values of fuels` average normal velocity and
 434 turbulent kinetic energy at the injection hole exit again increased with the increase in the fuels` mass
 435 flow rate. The peak values of average normal velocity and TKE at the hole exit again coincides with
 436 the time of the cavitation structures` occurrence. Figure 14 c indicates that cavitation influences
 437 conditions at the injection hole exit, and can influence fuel spray break-up further.

438 The timing of cavitation occurrence at the injection hole exit again depends on the fuel, and
439 coincides with the results of cavitation formation inside the injection hole for each tested fuel. This
440 indicates that lower fuel density and viscosity not only influence on cavitation formation inside the
441 injection hole, but also influence cavitation occurrence at the nozzle hole exit.

442 The second peak of TKE on Figure 13 b and Figure 14 b can be related to needle closing and late
443 appearance of cavitation structures in needle closing phase. During the needle closing phase
444 fluctuation in fuel flow can occur due to needle closing and can further result in second peak of TKE,
445 which is the highest in time of needle being almost fully closed.

446 **Conclusions**

447 In the presented paper the influence of pyrolytic oils, produced from waste plastic, were tested
448 numerically on fuel flow conditions inside the injection nozzle of a solenoid injector. First pyrolytic
449 oils were produced from waste HDPE and LDPE plastic using a single batch pyrolytic reactor. Then,
450 the properties of the obtained oils were determined using different test methods. The obtained oils`
451 properties were used further to specify 10%, 25% and 50% fuels mixtures properties with
452 conventional diesel fuel. All properties were further implemented in the AVL FIRE computational
453 program and used in the numerical study. The main conclusions from the presented study are:

- 454 - Pyrolytic oils obtained from waste HDPE and LDPE plastic have similar properties to
455 conventional diesel fuel.
- 456 - The lower viscosity of pyrolytic oils influences lower friction in the fuel nozzle flow, which
457 influences higher fuel velocity and compensates the lower fuel density`s influence on the
458 total injected fuel mass and mass flow rate.
- 459 - The lower density and viscosity of pyrolytic oils influence the more rapid formation and
460 spread of cavitation structures.
- 461 - Fuels with lower viscosity and density increase the amount of cavitation (vapor volume
462 fraction) at the injection hole exit and advance the time of its appearance.

- 463 - During the needle opening phase there is no significant difference at the nozzle hole outlet,
464 regardless of the fuel properties.
- 465 - The lower fuel viscosity and density of pure pyrolytic oils influence the shorter presence of
466 cavitation in the needle closing phase, lower resistance to disturbance and less choked flow
467 in the needle closing phase, which result in flow without cavitation fluctuation.
- 468 - Higher fuel viscosity and density influence the rebound cavitation formation close to the
469 injection hole walls.

470 From the presented study we can conclude that fuel properties have a significant influence on flow
471 conditions and cavitation formation inside the nozzle injection hole and at its exit. This can further
472 influence the spray break-up process, which is crucial for clean combustion optimal engine
473 performance. Cavitation structures can appear at the nozzle hole exit early in the injection process,
474 which can occur if pyrolytic oils are used. They can influence the faster decline of the spray axis,
475 which can cause formation of an asymmetrical fuel spray and increase the possibility for spray
476 collision with other spray or combustion chamber walls. The occurrence and fluctuation of cavitation
477 in the injection nozzle also influences the erosion of the injection hole. The erosion potential of each
478 fuel will be studied in further work.

479 Finally, the presented study indicates that plastic waste can be used for resource recovering, and can
480 help to reduce the environmental impact of plastic usage. In the presented study, we have confirmed
481 that high density and low density polyethylene can be converted into oils with similar properties to
482 conventional fuels using the pyrolytic process. The obtained pyrolytic oils can be used as a substitute
483 to conventional diesel fuel, but, due to their influence on the injection process, further studies are
484 needed before implementation.

485

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